

Lattice relaxation in $Zn_{1-x}Cd_xS$ binary alloy : An Extended X-ray Absorption Fine Structure (EXAFS) Study

Soham Mukherjee¹, Angshuman Nag¹, Pralay K. Santra¹, Mali Balasubramanian², Soma Chattopadhyay^{3,4}, Tomohiro Shibata^{3,4}, Franz Schaefer⁵, V. Kocevski⁶, J. Ruz⁶, C. Gerard⁶, O. Eriksson⁶, C.U. Segre⁴, and D.D. Sarma^{1,6}

¹ Solid State and Structural Chemistry Unit, Indian Institute of Science, Bangalore 560012, India

² X-ray Science Division, Argonne National Laboratory, Argonne, IL -60439, USA

³ MRCAT, Sector 10, Bldg 433B, Argonne, National Laboratory, Argonne, IL 60439 USA

⁴ CSRR & Department of Physics, Illinois Institute of Technology, Chicago, IL 60616 USA

⁵ Helmholtz-Zentrum Berlin für Materialien und Energie, Albert-Einstein-Strasse 15, D-12489 Berlin, Germany

⁶ Department of Physics and Astronomy, Uppsala University, Box 516, SE-751 20 Uppsala, Sweden

Introduction:-

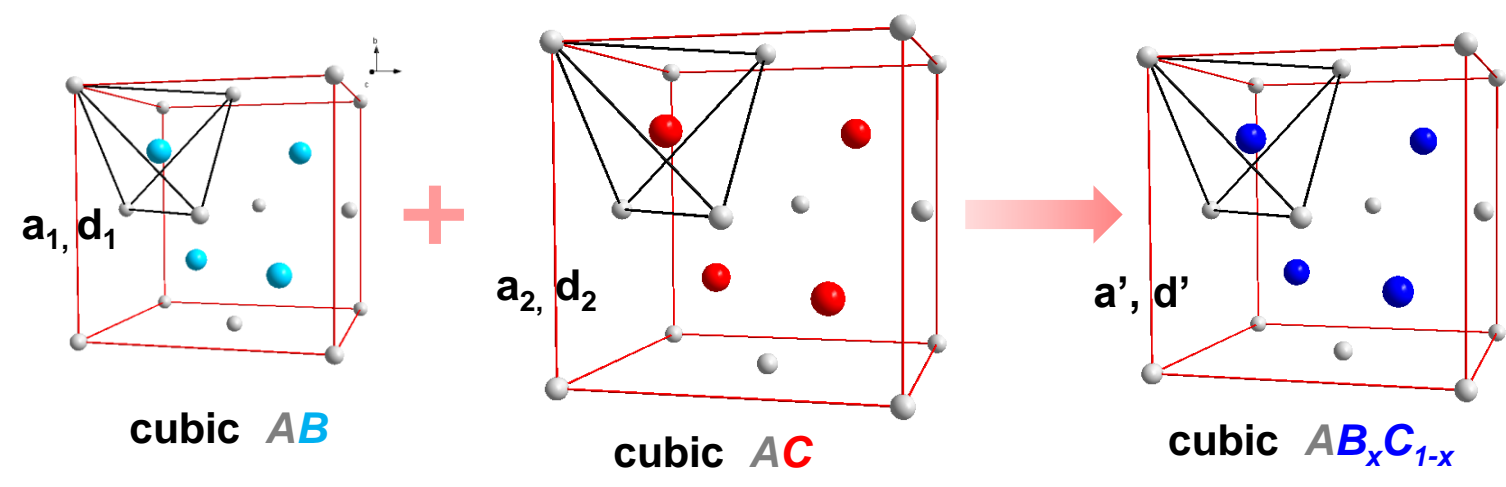
Vegard's Law :- A linear relation exists, at constant temperature, between the crystal lattice parameter of an alloy and the concentrations of the constituent end members; Thus, lattice parameters (a) of an alloy of the type AB_xC_{1-x} can be explained as a linear sum of its constituent members (AB and AC) in respective proportions

$$a_{AB_xC_{1-x}} = x.a_{AB} + (1-x).a_{AC}$$

Applicable to a wide range of alloys belonging to different crystal systems and different space groups

Background and Motivation :-

Virtual Crystal Approximation (VCA) :-



Global Structural Description :-

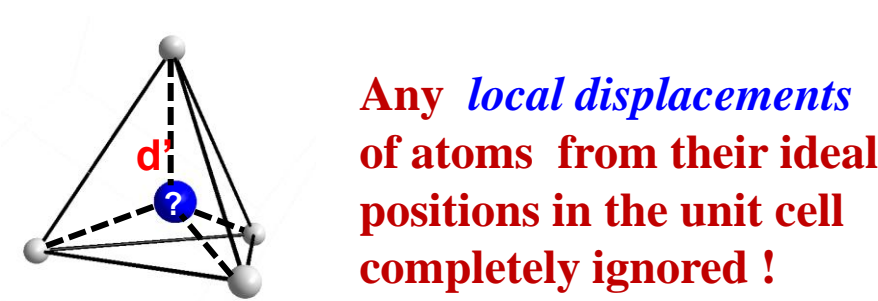
$$a' = x.a_1 + (1-x).a_2$$

$$d' = x.d_1 + (1-x).d_2$$

$$a' = nd'$$

Cell parameters
Bond Distances

Origin of the problem :-



Any local displacements of atoms from their ideal positions in the unit cell completely ignored!

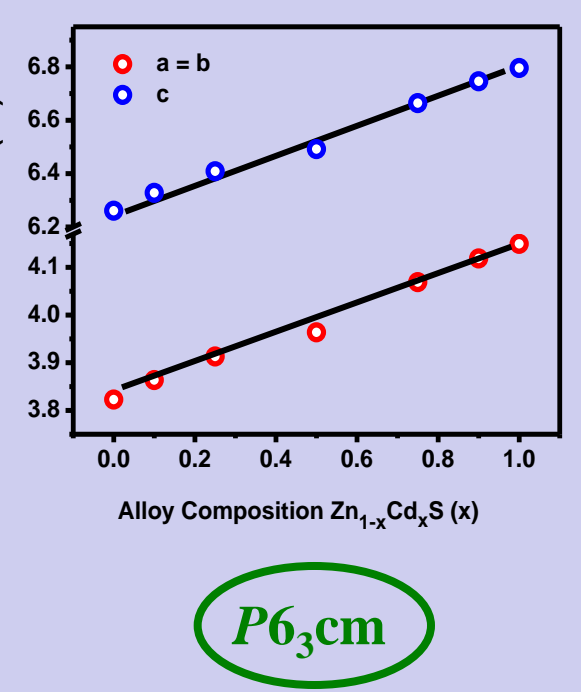
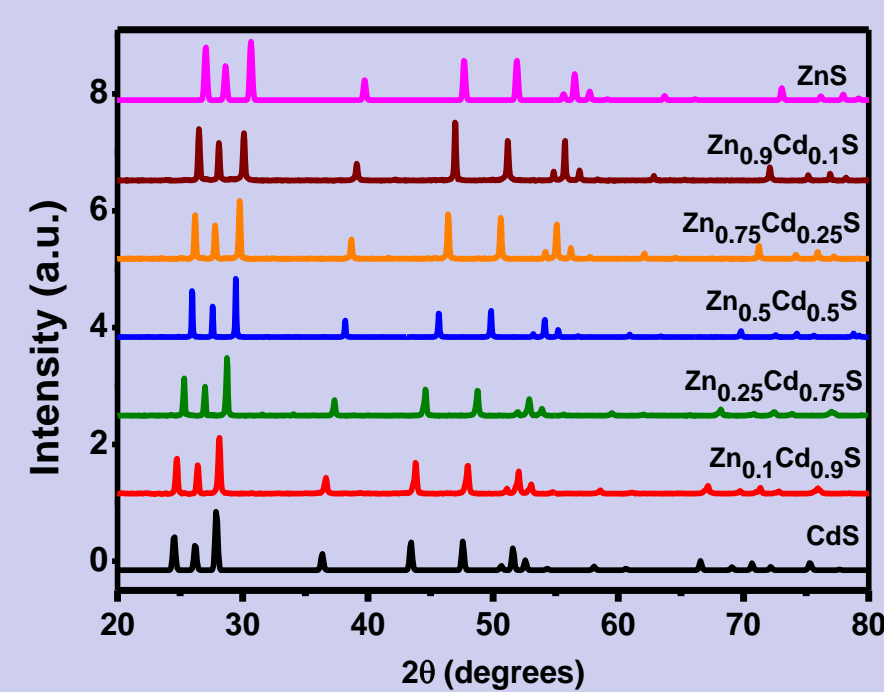
- Concept average bond length ?
- Distribution of atom-pair correlations ?
- Does the global crystal structure hold at the microscopic level ?

Aim of the study:-

- Detailed description of alloy structure at the atomic scale
- Is cationic substitution random in the alloy?
- Understand the nature of local alloying and relate it to the global description from diffraction

Results and discussion :-

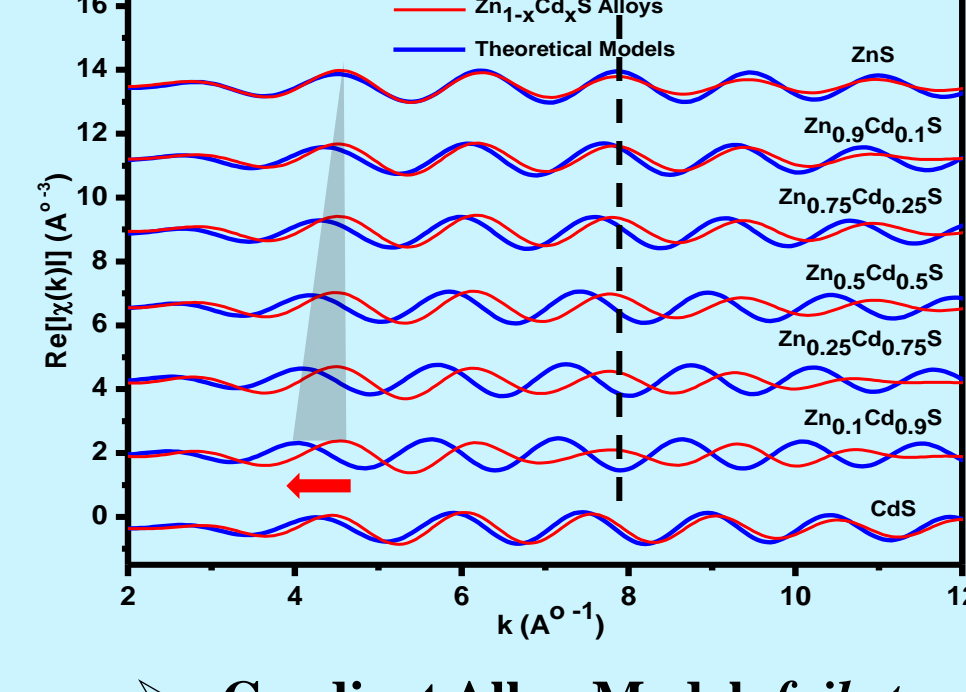
Success of Vegard's Law X-Ray diffraction (XRD)



$P6_3cm$

- $Zn_{1-x}Cd_xS$ alloys obey Vegard's Law

Failure of Vegard's Law Theoretical Simulations (EXAFS)

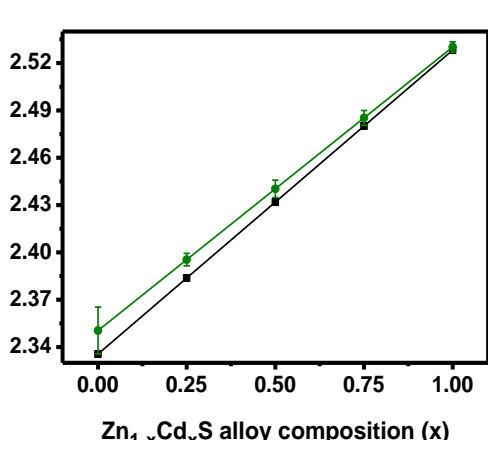
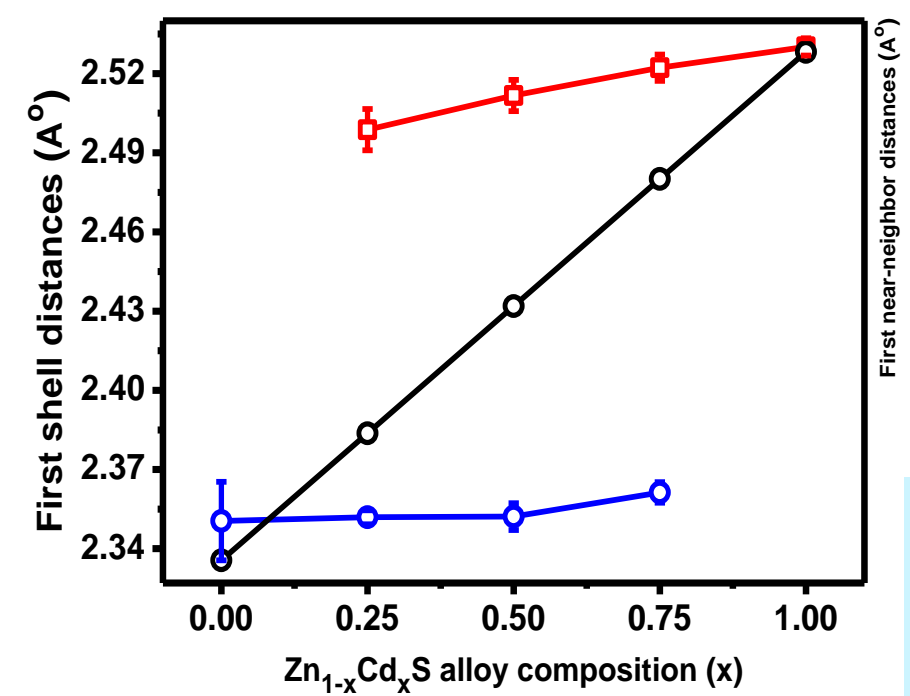


- Gradient Alloy Model fails to describe the local picture!

- Local structure markedly different from global structure
- EXAFS studies for local description of the alloy

First near-neighbor environment

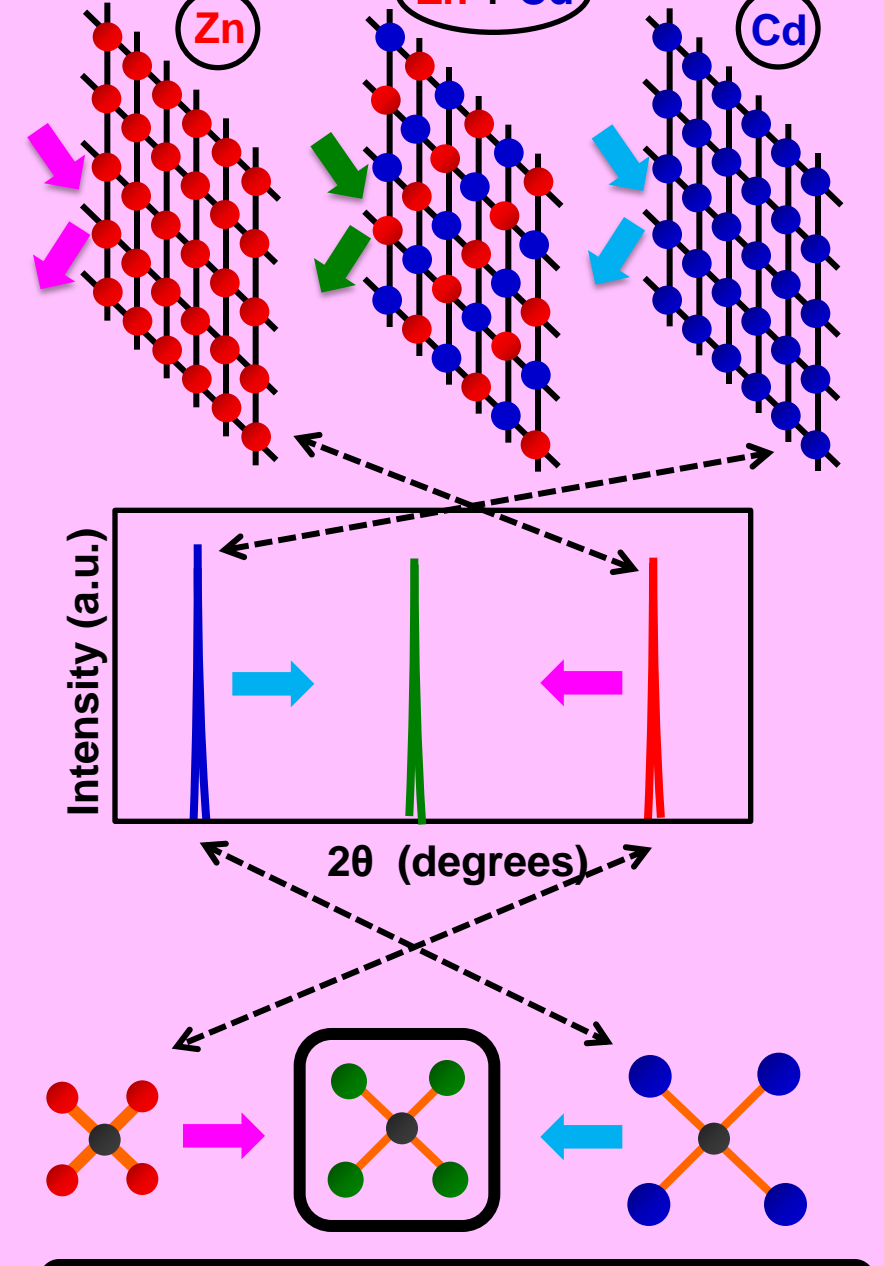
Bond distances :-



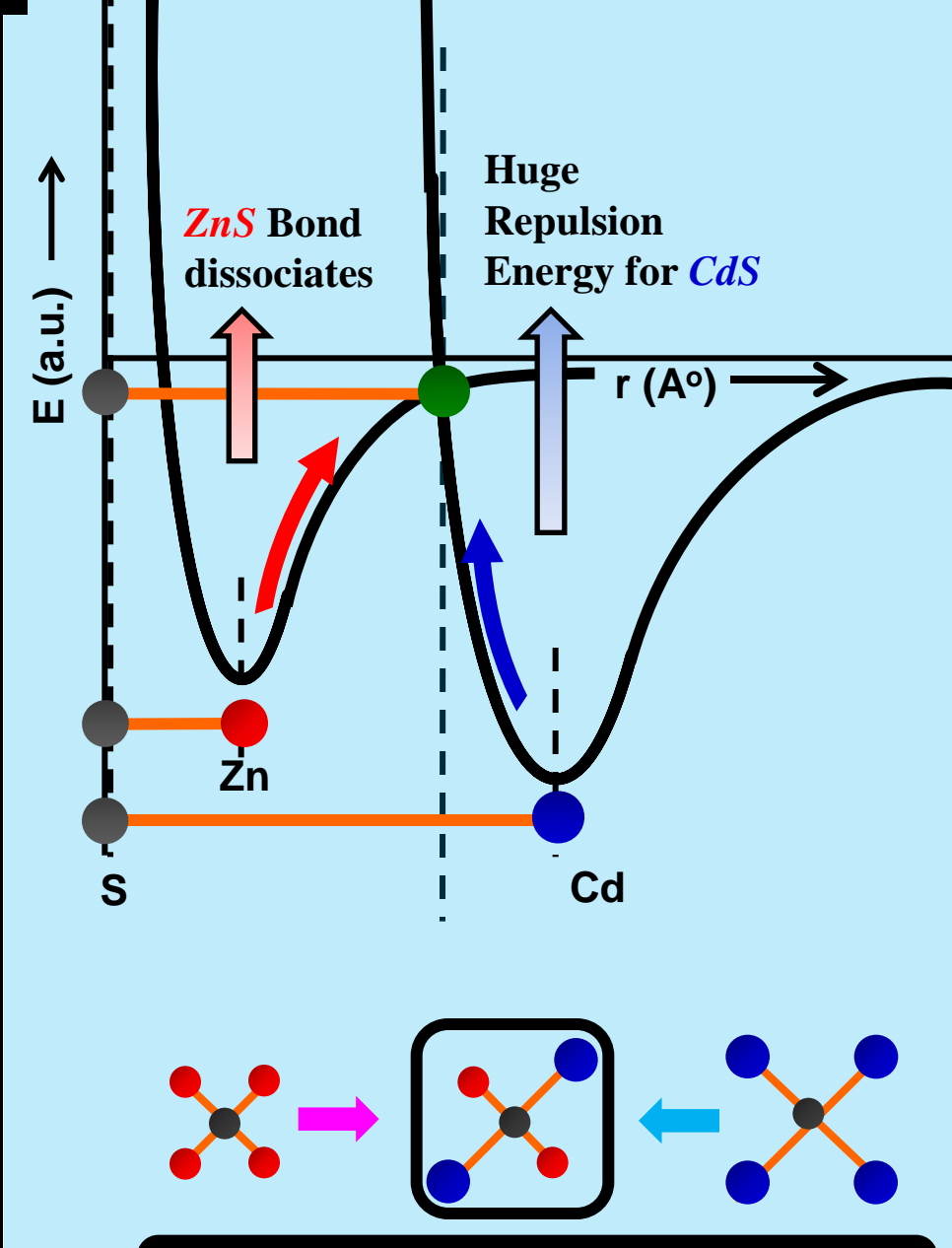
- Bimodal distribution of interatomic distances : Zn-S (Red) and Cd-S (Blue); Inset shows that average interatomic distance (Olive) closely approximates the virtual crystal line (Black)
- Bond lengths tend to retain their ideal crystallographic value and change only by 0.01-0.03 Å

- Small lattice dilation for by Zn-S (16.5%) and Cd-S (22.9%)
- Pseudo Debye-Waller factor (σ^2) dominated by static component

Atomic level scenario



Virtual Crystal | Real Crystal
Component Bond distances
Average Bond distance
 $\bar{d} = \frac{d_1 + d_2}{2}$
Bimodal bond distribution exists at the atomic level in a real crystal lattice



Bimodal bond distribution

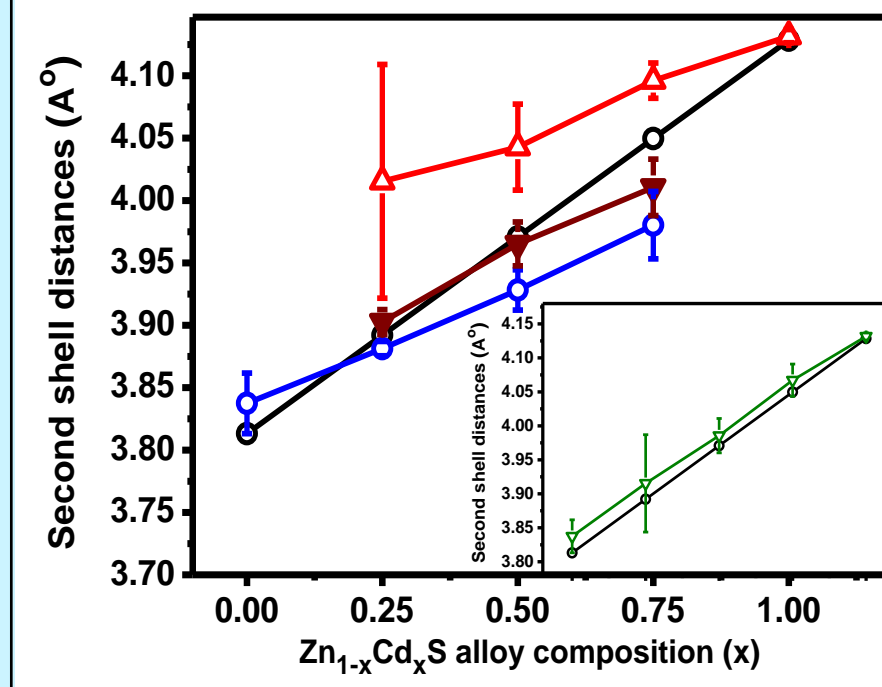
References :

- L. Vegard, Z. Phys. 5, 17 (1921).
J. C. Mikkelsen, Jr. and J. B. Boyce, Phys. Rev. B 28, 7130 (1983).
A. Balzarotti, N. Motta, A. Kiesel, M. Zimmel-Starnawska, M. T. Czyzyk, and M. Podgorny, Phys. Rev. B 31, 7526 (1985).
Z. Wu, K. Lu, Y. Wang, H. Li, C. Li, and Z. Fang, Phys. Rev. B 48, 8694 (1993).

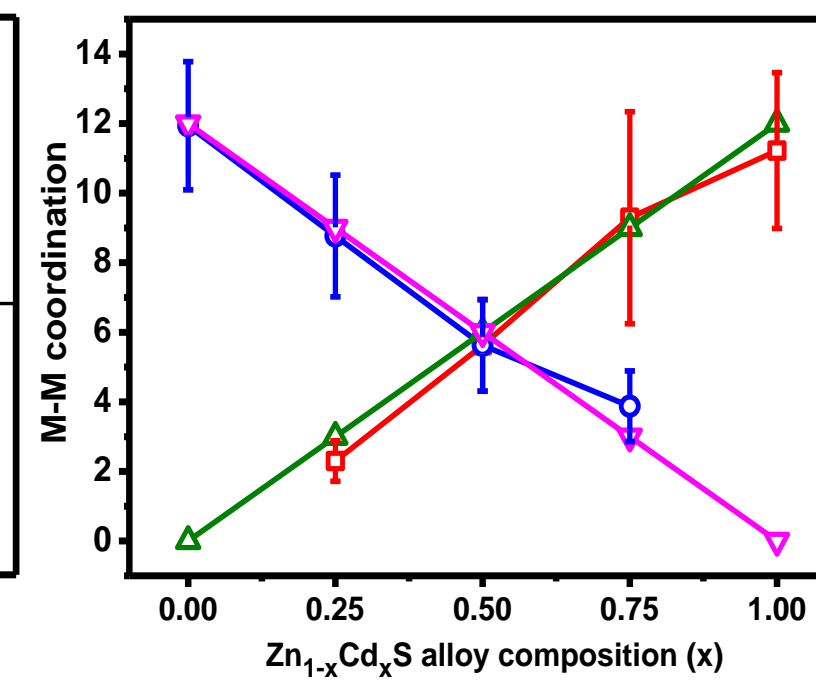
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Second near-neighbor environment

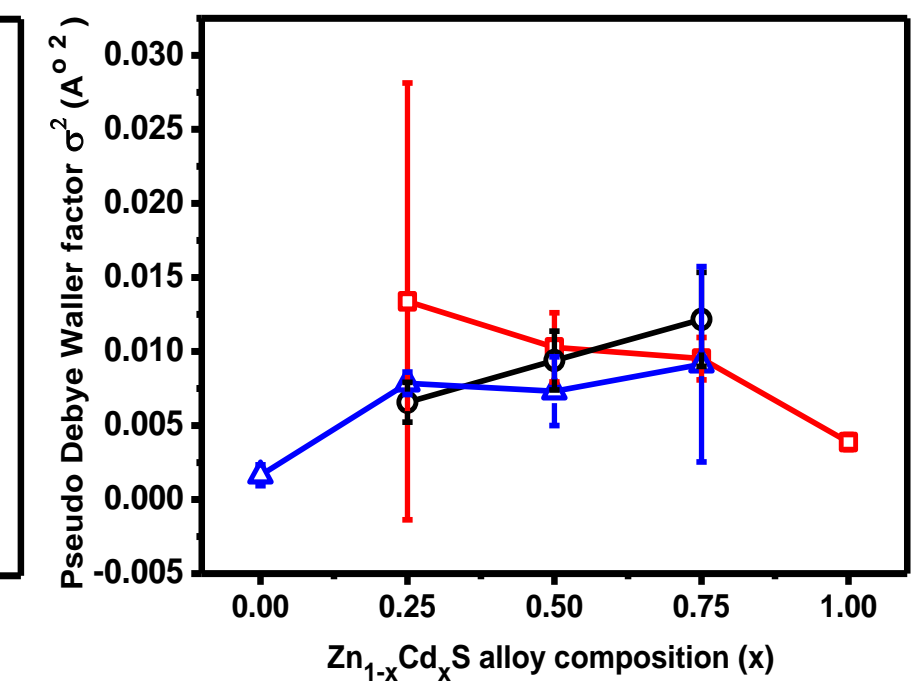
Bond distances :-



Homogeneity :-

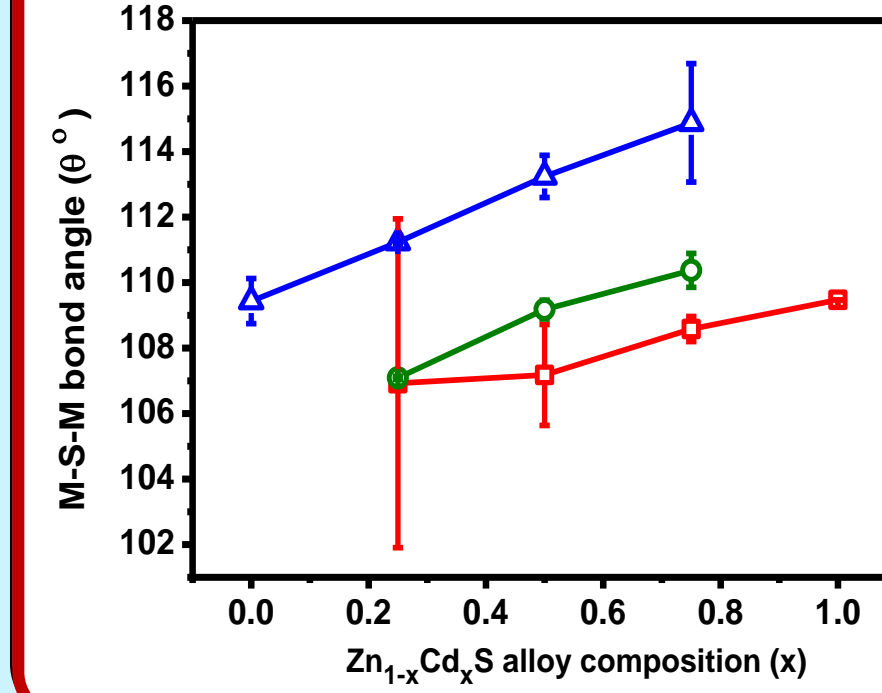


Disorder :-



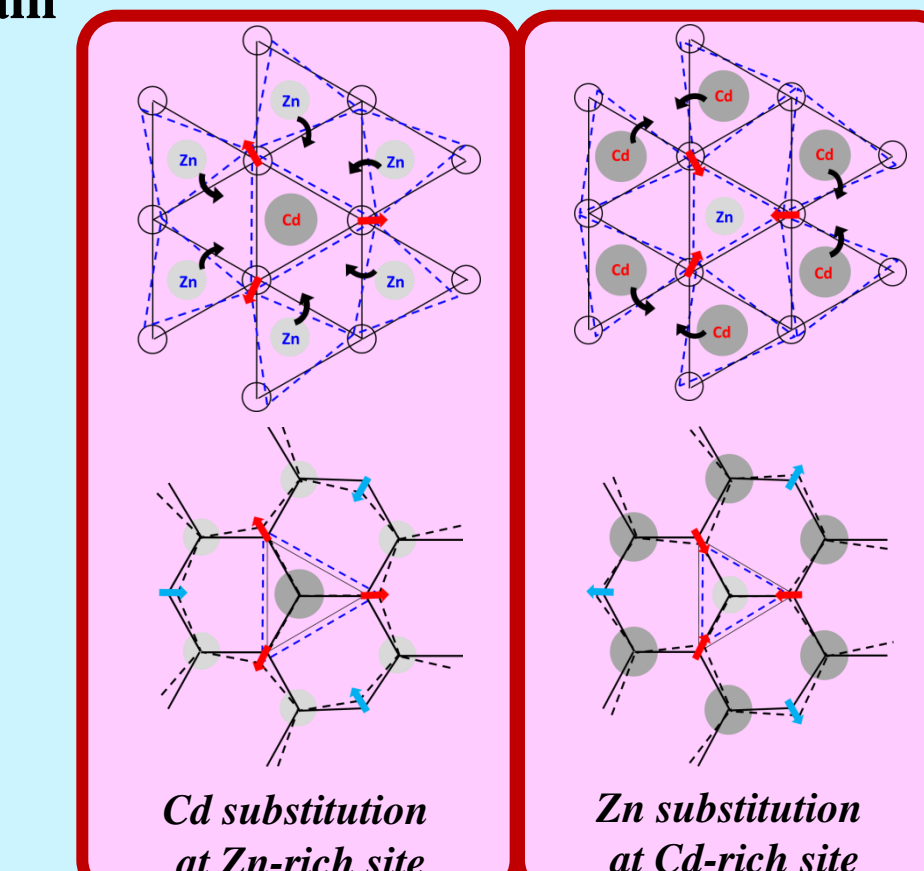
- Trimodal distribution of interatomic distances : Zn-S (Red), Zn-Cd (Wine) and Cd-S (Blue); Inset shows that average interatomic distance (Olive) closely approximates the virtual crystal line (Black)
- Random Alloy estimated from Zn:Cd ratio around Zn/Cd absorber; nominal Zn-Zn (pink), estimated Zn-Zn (Blue), nominal Cd-Cd (Olive) and estimated Cd-Cd (Red)
- σ^2 higher for alloys than pure end members due to competitive strain

Bond angles :-



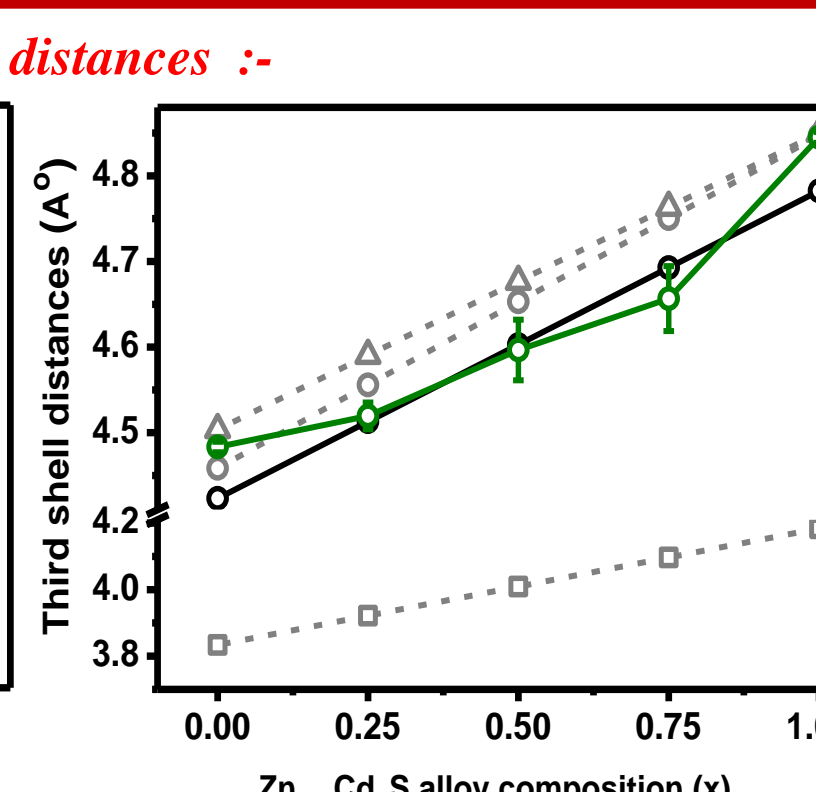
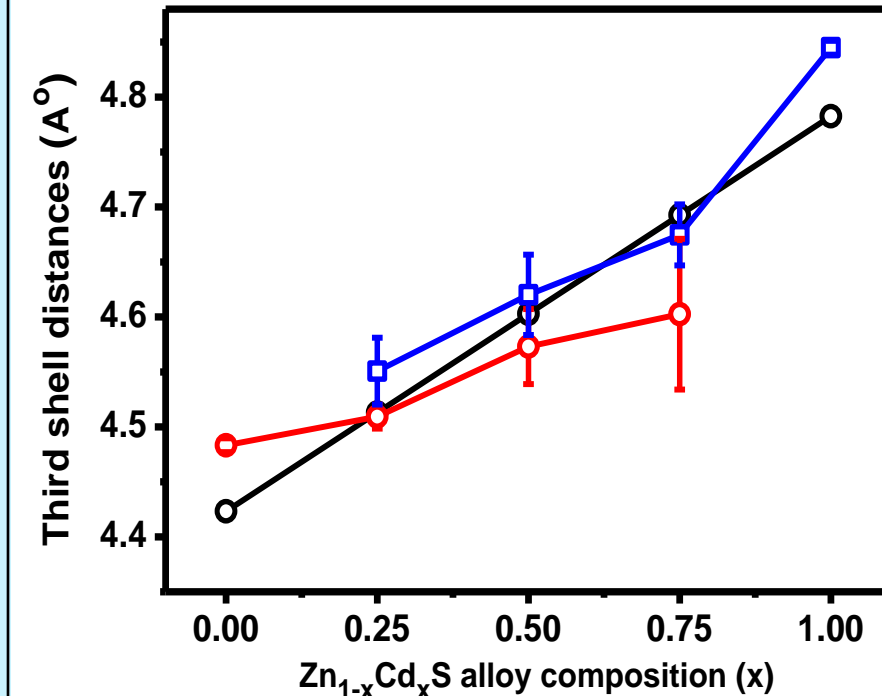
- Trimodal distribution of bond angles : Zn-S-Zn (Red), Zn-S-Cd (Olive); and Cd-S-Cd (Blue);

Competitive Strain on S sublattice

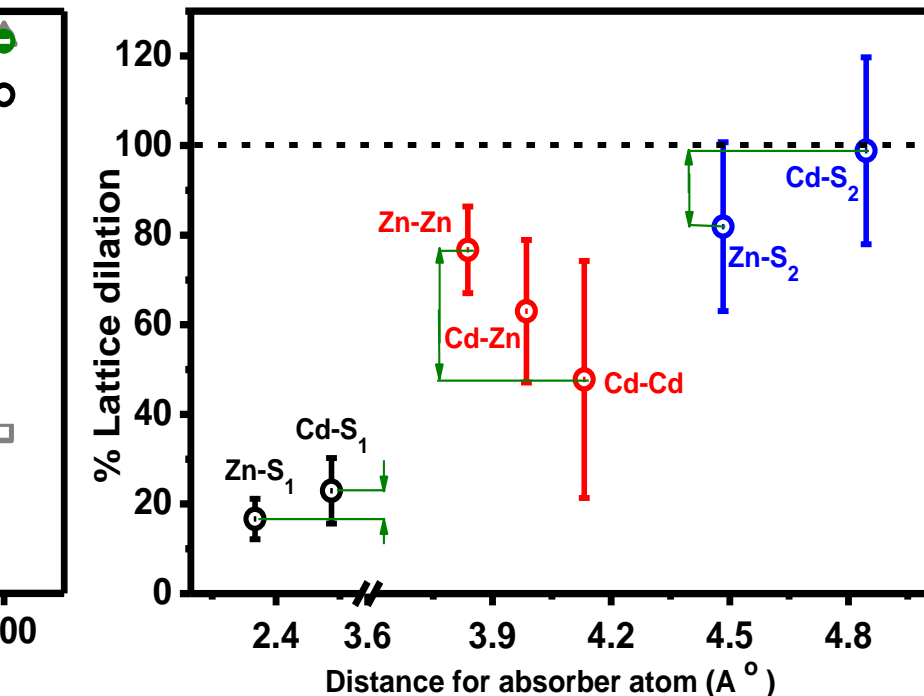


Third near-neighbor environment

Bond distances :-



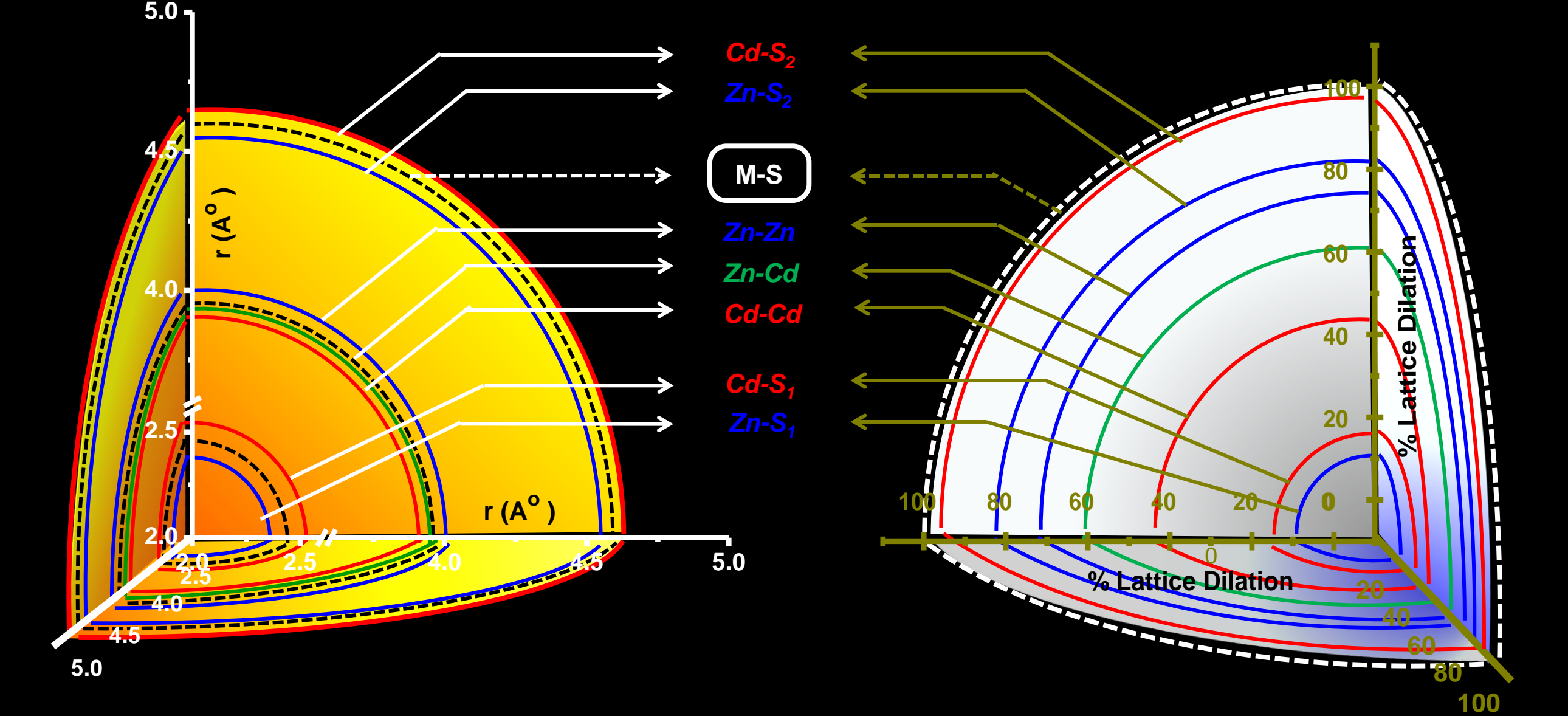
Coordination shell relaxation :-



- Zn-S (Red) and Cd-S (Blue) distances approach each other very closely and the average interatomic distance (Olive) closely approximates the virtual crystal line (Black) from XRD; grey lines represent different sets of M-S distances in virtual wurtzite crystal
- Large spatial separation for Zn-S and Cd-S intervened by a randomly substituted cationic sublattice yields high σ^2 values
- % lattice dilation increases with increasing distance from the absorber atom; differential atom-pair relaxation eventually merges with the virtual crystal relaxation line (Black dotted line)

Atom-pair spatial distribution

Differential lattice relaxation



Local structural description eventually merges with the global description (virtual) beyond third coordination sphere

Conclusions :

- Bimodal bond distribution in the first near neighbor for binary alloys obeying Vegard's Law with slight dilation; end member components tend to retain their identities locally at the atomic scale
- Trimodal distribution of cation-cation distances and angles shows with much stronger relaxation towards the virtual wurtzite crystal lattice owing to random alloying at the substituted cationic sublattice
- Zn-S and Cd-S correlations in third shell approach each other very closely and extent of dilation almost coincides with the average crystal line
- Lattice relaxation differentially increases with increasing distance of the scattering atom from the absorbing atom, finally merging with the virtual description beyond the third coordination shell
- Results from *ab initio* calculations on the systems are in good agreement with EXAFS results